

This is the relativity problem: to fix objectively a class of equivalent coordinatizations and to ascertain the group of transformations  $S$  mediating between them.

-- H. Weyl, *The Classical Groups*, Princeton Univ. Pr., 1946, p. 16

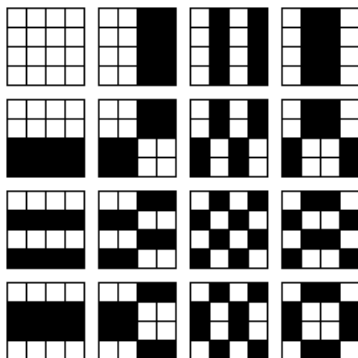
In finite geometry "points" are often defined as ordered  $n$ -tuples of a finite (i.e., Galois) field  $GF(q)$ . What geometric structures ("frames of reference," in Weyl's terms) are coordinatized by such  $n$ -tuples? Weyl's use of "objectively" seems to mean that such structures should have certain objective -- i.e., purely geometric -- properties invariant under each  $S$ .

This note suggests such a frame of reference for the affine 4-space over  $GF(2)$ , and a class of 322,560 equivalent coordinatizations of the frame.

**The frame:** A 4x4 array.

**The invariant structure:**

The following set of 15 partitions of the frame into two 8-sets.



**A representative coordinatization:**

```
0000 0001 0010 0011
0100 0101 0110 0111
1000 1001 1010 1011
1100 1101 1110 1111
```

**The group:** The group  $AGL(4,2)$  of 322,560 regular affine transformations of the ordered 4-tuples over  $GF(2)$ .